

Diocesan Boys' School
2021-2022 Grade 12 Mock Examination
Mathematics Compulsory Part
Paper 2

Suggested Solution

1. D

$$= \frac{3^{4m} \cdot 3^{4m}}{3^{6m}}$$

$$= 3^{2m}$$

2. D

$$-pq - p^2 = -3p + 3q$$

$$3p - p^2 = 3q + pq$$

$$\frac{3p - p^2}{3 + p} = q$$

$$q = \frac{p(3-p)}{3+p}$$

3. C

$$= (2-q)(p+2q)(-2)(p-2q)$$

$$= (-4+2q)(p^2 - 4q^2)$$

$$= -4p^2 + 16q^2 + 2p^2q - 8q^3$$

4. A

$$= \frac{-3(6-x) - 5(x-4)}{(x-4)(6-x)}$$

$$= \frac{-18 + 3x - 5x + 20}{(x-4)(6-x)}$$

$$= \frac{-2(x-1)}{(x-4)(6-x)}$$

5. C
Sub $x = -2$
 $-3a + c = 0$
 $3a = c$
 $a : c = 1 : 3$

6. D

$$= 3(\beta-1)^2 - \alpha(\beta-1) + 1$$

$$-3(\beta+1)^2 + \alpha(\beta+1) - 1$$

$$= 3(-2\beta - 2\beta) + 2\alpha$$

$$= -12\beta + 2\alpha$$

7. D

$$p(x) = (x^2 - 4)q(x) + ax + b$$

$$\begin{aligned} & \begin{cases} p(-2) = 8 \\ p(2) = 0 \end{cases} \\ \Rightarrow & \begin{cases} -2a + b = 8 \\ 2a + b = 0 \end{cases} \\ \Rightarrow & \begin{cases} a = -2 \\ b = 4 \end{cases} \end{aligned}$$

8. C
no. of foreigners
 $= 150(20\%)$
 $= 30$
no. of female foreigners
 $= 30 - 12$
 $= (1 - 75\%)(\text{no. of female})$

no. of female
 $= 72$
no. of male
 $= 150 - 72$
 $= 78$

no. of local male
 $= 78 - 12$
 $= 66$
9. C
 $1 - 2x \geq 3x - 9$ or $-7x \geq 14$
 $10 \geq 5x$ $x \leq -2$
 $x \leq 2$

$\Rightarrow x \leq 2$

10. C
 $16p + 12r = 6p + 27r$
 $10p = 15r$
 $2p = 3r$
 $p:r = 3:2 = 9:6$

$$q:r = 4:3 = 8:6$$

$$p:q:r = 9:8:6$$

$$(p+q):(q-r) = 17:2$$

11. D
 $v = \frac{k\sqrt{x}}{y^2}$

$$v' = \frac{k\sqrt{1.21x}}{0.1^2 y^2} = 110v$$

% change
 $= \left(\frac{110v - v}{v} \right) (100\%)$
 $= 10900\%$

12. C
 $a_7 = 2a_5 - a_6$
 $a_7 = 10 - a_6$
 $a_6 = 10 - a_7$

$$a_8 = 2a_6 - a_7$$

$$-7 = 2(10 - a_7) - a_7$$

$$a_7 = 9$$

13. A
 $S > 2.5 \cdot 3.5 + [(3.5 - 1.5) + 3.5](4.5 - 2.5) \left(\frac{1}{2} \right)$
 $S > 14.25$
and

$$S < 3.5 \cdot 4.5 + [(4.5 - 0.5) + 4.5](5.5 - 3.5) \left(\frac{1}{2} \right)$$

$$S < 24.25$$

14. C
I: False
Sum of root = $0 + 10 = \frac{-b}{a}$
 $\Rightarrow ab < 0$

II: True
 $c = 0$

III: True
Sub (10,0)
 $0 = 100a + 10b + 0$
 $0 = 10a + b$
 $\therefore a < 0$
 $\therefore 8a + b > 0$

15. C
 $h^2 = 25^2 - (20^2 + 9^2)$
 $h = 12$

Total surface area
 $= (20)(9)(2) + (20+9)(2)(12)$
 $= 1056$

16. A
 $\pi(8k)^2 + \pi(8k)(17k) = 50\pi$
 $200k^2 = 50$
 $k = 0.5$

$$r = 4$$

$$l = \frac{17}{2}$$

$$h = \sqrt{l^2 - r^2} = 7.5$$

Volume
 $= \pi(4^2)(7.5) \left(\frac{1}{3} \right)$
 $= 40\pi$

17. A
In $\triangle DCO$

$$\cos \angle DOC = \frac{r}{2r}$$

$$\angle DOC = 60^\circ$$

$$\sin 60^\circ = \frac{6\sqrt{3}}{DO}$$

$$DO = 12$$

$$60^\circ + \angle OBA = 105^\circ$$

$$\angle OBA = 45^\circ$$

$$\angle OAB = 45^\circ$$

In $\triangle AEO$

$$45^\circ + 105^\circ + \angle EOA = 180^\circ$$

$$\angle EOA = 30^\circ$$

Area

$$= \pi(12)^2 \left(\frac{30^\circ}{360^\circ} \right)$$

$$= 12\pi$$

18. C
 $\triangle BCE \cong \triangle DCF$ (S.A.S.)
 $\triangle AEC \cong \triangle AFC$ (S.S.S.)

$$\angle EAF + 80^\circ = 180^\circ$$

$$\angle EAF = 100^\circ$$

$$\angle AEC + \frac{100^\circ}{2} + \frac{42^\circ}{2} = 180^\circ$$

$$\angle AEC = 109^\circ$$

19. D
I: True
 \because Symmetry
 \Rightarrow Congruent

II: True
 \because Regular
 $\therefore FE \parallel AH$ and $AF \parallel HE$
 $\therefore AH \parallel HD$
 $\Rightarrow FE = HD$

$$\because \angle FIE = \angle HID \quad \text{vert.opp } \angle s$$

$\because \angle FEI = \angle IHD$ alt $\angle s$, $FE \parallel AD$
 $\therefore \triangle EFI \cong \triangle HDI$ A.A.S.
 $\therefore \triangle EFI \cong \triangle HDI \cong \triangle HBG$

III. True
 $\because \angle FGA = \angle EID = 90^\circ$
 $\because AF = DE$
 $\therefore \angle FAG = \angle IED$
A.A.S.

20. C
Consider the area of

$$\triangle DBE : \triangle ABC = 2^2 : (2+3)^2$$

$$\triangle DBE = 72$$

$$\triangle DBE : \triangle ADF = 2^2 : 3^2$$

$$\triangle ADF = 162$$

$$\triangle ECF = 450 - 72 - 162 = 216$$

21. D
I: False
 $HC \neq CF$

II: True

III: True
 $\angle GCD = \frac{(5-2)(180^\circ) - 3(140^\circ)}{2} = 60^\circ$
 $\angle ICH = \frac{180^\circ - 140^\circ}{2} = 20^\circ$

22. C
 $\angle BAE + 68^\circ = 180^\circ$

$$\angle BAE = 112^\circ$$

$$\angle EBD + 68^\circ + 90^\circ = 180^\circ$$

$$\angle EBD = 22^\circ$$

$$\angle AEB = \angle EBD = 22^\circ$$

$$\angle ABE + 112^\circ + 22^\circ = 180^\circ$$

$$\angle ABE = 46^\circ$$

$$\angle ACE = \angle ABE = 46^\circ$$

23. D
 $R : (-5, -1)$
 $Q : (1, -5)$
 $P : (5, -5)$

24. A

$$\cos \alpha = \frac{3k + 5k}{CE}$$

$$CE = \frac{8k}{\cos \alpha}$$

$$\cos \beta = \frac{k + 3k}{DF}$$

$$DF = \frac{4k}{\cos \beta}$$

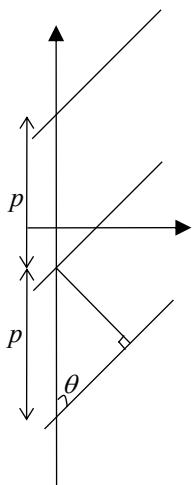
$$CE : DF = \frac{8k}{\cos \alpha} : \frac{4k}{\cos \beta} = 2 \cos \beta : \cos \alpha$$

25. B
 $\tan \theta = a$

$$\theta = 45^\circ$$

$$\sin \theta = \frac{\sqrt{2}}{p}$$

$$p = 2$$



26. B
I: True
 $L_1 : y = -\frac{1}{a}x - 1$

$$-\frac{1}{a} > 0 \\ a < 0$$

II: False

$$L_2 : y = -cx - b \\ -1 = -b \\ b = 1 \neq a$$

III: True

$$PQ > 2OP \\ OQ > OP \\ \frac{1}{c} > -a \\ 1 > -ac \quad \therefore c > 0 \\ ac > -1$$

27. D
 $H : (2, -1)$

$$K : (2, 4)$$

A: False

$$\text{Put } (0, 0) \\ LHS = 55 > 0$$

B: False

$$3 = \sqrt{2^2 + 1^2 + 4} > \sqrt{2^2 + 4^2 - \frac{55}{4}} = 2.5$$

C: False

$$HK = 5 \neq 5.5 = (3 + 2.5)$$

D: True

$$(m_{OH})(m_{OK}) = \left(\frac{-1}{2}\right)\left(\frac{4}{2}\right) = -1$$

28. B
 $0 \leq b \leq 4$

$$p = \frac{4}{20} = 0.2$$

29. A

A: True

$$IQR = 26 - 20 = 6$$

B: Cannot be determined

C: False

Consider 16,20,24,26,30

$$\text{Less than } \$24 := \frac{2}{5}$$

D: False

Consider 16,20,24,26,30

$$\text{More than } \$26 := \frac{1}{5} = 20\%$$

30. D

All True

31. B

Third Expression:

Coeff : 1,2,3,6

Power of x : 2,3,4

Power of y : 2

Power of z : 0

32. B

$$\begin{aligned}
 &= 8^{10} + 7(8) + 12(16^8) + 14(16) \\
 &= 2^{30} + 7(2^3) + 3(2^{34}) + 7(2^5) \\
 &= 2^{30} + 48(2^{30}) + 7(2^3) + 28(2^3) \\
 &= 49(2^{30}) + 35(2^3)
 \end{aligned}$$

33. B

I: True

Consider $x = 1$,

$$a > b$$

II: True

Put $y = c$,

$$x_b = \frac{\log c}{\log b}$$

$$BC = -\frac{\log c}{\log b}$$

$$x_a = \frac{\log c}{\log a}$$

$$AC = \frac{\log c}{\log a}$$

Note that $0 < b < 1 < a$

$$BC > AC > 0$$

$$-\frac{\log c}{\log b} > \frac{\log c}{\log a} > 0$$

$$-\log a < \log b < 0$$

$$-1 < \log_a b < 0$$

$$a^{-1} < b < a^0$$

$$1 < ab < 0$$

III: False

$$\begin{aligned}
 &\frac{AC}{BC} \\
 &= \frac{\log c}{\log a} \div \left(-\frac{\log c}{\log b} \right) \\
 &= -\frac{\log b}{\log a} \\
 &= -\log_a b
 \end{aligned}$$

34. A

$$\log_4 y = \log_4 8 + \log_4 \sqrt{x}$$

$$\log_4 y = \frac{3}{2} + \frac{1}{2} \log_4 x$$

$$\text{vertical_int} = \frac{3}{2}$$

$$\text{horizontal_int} = -3$$

$$\text{Product} = -\frac{9}{2}$$

35. A

$$= -1 - \frac{5a(-i)}{2+i}$$

$$= -1 + \frac{5ai(2-i)}{4-(-1)}$$

$$= -1 + 2ai + a$$

36. B

I: False

$$T(2) - T(1) = 2a \neq a = T(3) - T(2)$$

II: True

$$2\log a, 3\log a, 4\log a$$

III: False

when $a = 90^\circ$

37. B

Least value at (3,6)

$$= 11(3) - 5(6) = 3$$

38. B

$$CE^2 = 20^2 + 20^2 - 2(20^2)\cos 108^\circ$$

$$CE = 32.36067977$$

$$CG^2 = 20^2 + CE^2 - 2(20)(CE)\cos 18^\circ$$

$$CG = 14.70170673$$

$$20^2 = CG^2 + CE^2 - 2(CG)(CE)\cos \angle ECG$$

$$\angle ECG = 24.85873723$$

$$\angle EIC$$

$$= 180^\circ - 36^\circ - \angle ECG$$

$$= 119.1412328^\circ$$

$$\frac{CI}{\sin 36^\circ} = \frac{CE}{\sin \angle EIC}$$

Area

$$= \left(\frac{1}{2}\right)(CI)(CE)\sin \angle ECG$$

$$= 148.1305253$$

39. B

$$\widehat{BC} : \widehat{CD} : \widehat{AD} = 3 : 6 : 9$$

Let

$$\angle BAC = x$$

$$\angle CAD = 2x$$

$$\angle ACD = 3x$$

$$\angle BCD + \angle DAB = 180^\circ$$

$$(90^\circ + 3x) + (2x + x) = 180^\circ$$

$$x = 15^\circ$$

$$\angle AEC = \angle BAC = x$$

$$46^\circ + 3x + 2x + \angle DAE + x = 180^\circ$$

$$\angle DAE = 44^\circ$$

40. B

In ΔPQR ,

$$PR = \frac{PQ}{\sin 45^\circ} = \frac{2PQ}{\sqrt{2}}$$

$$QR = \frac{PQ}{\tan 45^\circ} = PQ$$

In ΔPQS ,

$$PS = \frac{PQ}{\sin 60^\circ} = \frac{2PQ}{\sqrt{3}}$$

$$QS = \frac{PQ}{\tan 60^\circ} = \frac{PQ}{\sqrt{3}}$$

In ΔQRS ,

$$RS^2 = QR^2 + QS^2 - 2(QR)(QS)\cos 120^\circ$$

$$RS^2 = (PQ^2) \left[1 + \frac{1}{3} - 2 \left(\frac{1}{\sqrt{3}} \right) \cos 120^\circ \right]$$

$$RS^2 = (PQ^2)(1.910683603)$$

In ΔPRS ,

$$RS^2 = PR^2 + PS^2 - 2(PR)(PS)\cos \angle RPS$$

$$RS^2 = PQ^2 \cdot \left[\frac{4}{2} + \frac{4}{3} - 2 \left(\frac{2}{\sqrt{2}} \right) \left(\frac{2}{\sqrt{3}} \right) \cos \angle RPS \right]$$

$$\angle RPS \approx 64^\circ$$

41. B

$$\left(-\frac{4}{3} \right) \begin{vmatrix} 0 & -\frac{3}{2} \\ \frac{r_x}{2} & -0 \end{vmatrix} = -1$$

$$r_x = -2$$

42. A

P(win at the first draw)

$$= \frac{1}{2} + \left(\frac{1}{2} \right) \left(\frac{4}{8} \right) = \frac{3}{4}$$

P(Lok win)

$$= \left(\frac{1}{4} \right) \left(\frac{3}{4} \right) + \left(\frac{1}{4} \right)^3 \left(\frac{3}{4} \right) + \left(\frac{1}{4} \right)^5 \left(\frac{3}{4} \right) + \dots$$

$$= \left(\frac{1}{4} \right) \left(\frac{3}{4} \right) \left[1 + \left(\frac{1}{4} \right)^2 + \left(\frac{1}{4} \right)^4 + \left(\frac{1}{4} \right)^6 + \dots \right]$$

$$= \left(\frac{3}{16} \right) \left[\frac{1}{1 - \frac{1}{16}} \right]$$

$$= \frac{1}{5}$$

43. D

$$\frac{\left(\frac{6}{11} \right) \left(\frac{5}{10} \right) \left(\frac{4}{9} \right) \left(\frac{3}{8} \right) \left(\frac{5}{7} \right)}{\left(\frac{6}{11} \right) \left(\frac{5}{10} \right) \left(\frac{4}{9} \right)} = \frac{15}{56}$$

44. A

$$\frac{70 - \mu}{x} = 0.8$$

$$\mu = 70 - 0.8x$$

$$\frac{D - \mu}{x} = -1.2$$

$$D = \mu - 1.2x$$

$$D = 70 - 0.8x - 1.2x$$

45. A

I: False

$$x_1 = a + 24d$$

$$x_2 = a + 24.5d$$

d can be negative

II: True

$$x_2 = a + 24.5d = y_2$$

III: False

if $d = 0$,

$$z_1 = z_2$$