2016-DSE MATH CP PAPER 2

HONG KONG EXAMINATIONS AND ASSESSMENT AUTHORITY
HONG KONG DIPLOMA OF SECONDARY EDUCATION EXAMINATION 2016

MATHEMATICS Compulsory Part PAPER 2

11.30 am - 12.45 pm (11/4 hours)

INSTRUCTIONS

- 1. Read carefully the instructions on the Answer Sheet. After the announcement of the start of the examination, you should first stick a barcode label and insert the information required in the spaces provided. No extra time will be given for sticking on the barcode label after the 'Time is up' announcement.
- 2. When told to open this book, you should check that all the questions are there. Look for the words 'END OF PAPER' after the last question.
- 3. All questions carry equal marks.
- 4. ANSWER ALL QUESTIONS. You are advised to use an HB pencil to mark all the answers on the Answer Sheet, so that wrong marks can be completely erased with a clean rubber. You must mark the answers clearly; otherwise you will lose marks if the answers cannot be captured.
- 5. You should mark only **ONE** answer for each question. If you mark more than one answer, you will receive **NO MARKS** for that question.
- 6. No marks will be deducted for wrong answers.

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Not to be taken away before the end of the examination session

There are 30 questions in Section A and 15 questions in Section B. The diagrams in this paper are not necessarily drawn to scale. Choose the best answer for each question.

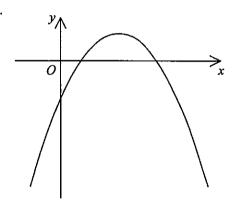
Section A

- 1. $8^{222} \cdot 5^{666} =$
 - A. 10⁶⁶⁶.
 - B. 10⁸⁸⁸.
 - C. 40⁶⁶⁶.
 - D. 40⁸⁸⁸ .
- 2. If $\frac{a}{x} + \frac{b}{y} = 3$, then x =
 - A. $\frac{ay}{3y-b}$.
 - B. $\frac{ay}{b-3y}$.
 - C. $\frac{by}{3y-a}$.
 - D. $\frac{by}{a-3y}$.
- 3. $16-(2x-3y)^2 =$
 - A. (4-2x-3y)(4+2x+3y).
 - B. (4-2x-3y)(4+2x-3y).
 - C. (4-2x+3y)(4+2x+3y).
 - D. (4-2x+3y)(4+2x-3y).

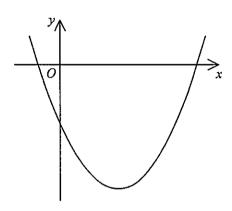
- 4. 0.0765403 =
 - A. 0.076 (correct to 2 significant figures).
 - B. 0.0765 (correct to 3 decimal places).
 - C. 0.07654 (correct to 4 significant figures).
 - D. 0.076540 (correct to 5 decimal places).
- 5. If $4\alpha + \beta = 7\alpha + 3\beta = 5$, then $\beta =$
 - A. -3.
 - B. -2.
 - C. 2.
 - D. 3.
- 6. Let $f(x) = 4x^3 + kx + 3$, where k is a constant. If f(x) is divisible by 2x + 1, find the remainder when f(x) is divided by x + 1.
 - A. –7
 - В. –6
 - C. 0
 - D. 5
- 7. The solution of -5x > 21 2x and 6x 18 < 0 is
 - A. x < -7.
 - B. x < 3.
 - C. -7 < x < 3.
 - D. x < -7 or x > 3.

- 8. If k is a constant such that the quadratic equation $x^2 + kx + 8k + 36 = 0$ has equal roots, then k =
 - А. -6.
 - B. 12.
 - C. -4 or 36.
 - D. -18 or 2.
- 9. If -1 < a < 0, which of the following may represent the graph of $y = (ax + 1)^2 + a$?

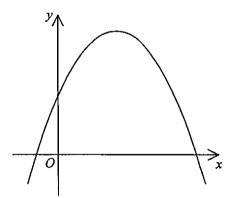
A.



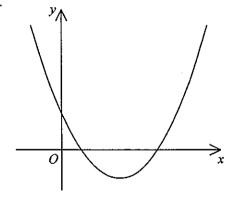
B.



C.

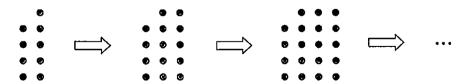


D.



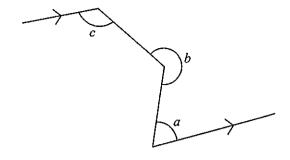
- 10. The monthly salary of Donald is 25% higher than that of Peter while the monthly salary of Peter is 25% lower than that of Teresa. It is given that the monthly salary of Donald is \$33360. The monthly salary of Teresa is
 - A. \$31275.
 - B. \$33360.
 - C. \$35584.
 - D. \$52125.

- 11. If x and y are non-zero numbers such that (3y-4x):(2x+y)=5:6, then x:y=
 - A. 7:8.
 - B. 8:29.
 - C. 9:32.
 - D. 13:34.
- 12. It is given that z varies directly as \sqrt{x} and inversely as y. If x is decreased by 36% and y is increased by 60%, then z
 - A. is increased by 24%.
 - B. is increased by 28%.
 - C. is decreased by 40%.
 - D. is decreased by 50%.
- 13. The cost of flour of brand X is 42/kg. If 3 kg of flour of brand X and 2 kg of flour of brand Y are mixed so that the cost of the mixture is 36/kg, find the cost of flour of brand Y.
 - A. \$27/kg
 - B. \$30/kg
 - C. \$32/kg
 - D. \$39/kg
- 14. In the figure, the 1st pattern consists of 9 dots. For any positive integer n, the (n+1) th pattern is formed by adding 5 dots to the nth pattern. Find the number of dots in the 7th pattern.

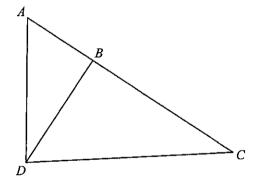


- A. 29
- B. 34
- C. 39
- D. 44

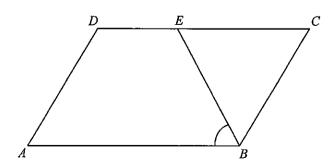
- 15. According to the figure, which of the following must be true?
 - I. $a+c=180^{\circ}$
 - II. $a+b-c=180^{\circ}$
 - III. $b+c=360^{\circ}$
 - A. I only
 - B. II only
 - C. I and III only
 - D. II and III only



- 16. In the figure, ABC is a straight line. If AB = 24 cm , AD = 40 cm , BD = 32 cm and CD = 68 cm , then BC =
 - A. 43 cm.
 - B. 54 cm.
 - C. 55 cm.
 - D. 60 cm.



- 17. In the figure, ABCD is a parallelogram. E is a point lying on CD such that BE = CE. If $\angle ADC = 114^{\circ}$, then $\angle ABE =$
 - A. 48°.
 - B. 57°.
 - C. 62°.
 - D. 66°.



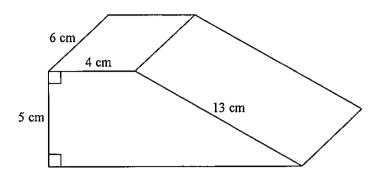
18. The figure shows a right prism. Find the volume of the prism.







D. 328 cm³



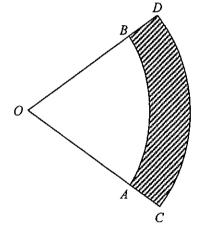
- 19. In the figure, OAB and OCD are sectors with centre O, where OA = 33 cm and OC = 39 cm. The area of the shaded region ABDC is 72π cm². Which of the following is/are true?
 - I. The angle of the sector OAB is 60° .
 - II. The area of the sector OAB is 11π cm².
 - III. The perimeter of the sector OCD is 13π cm.



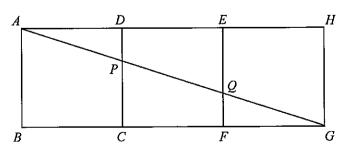
B. II only

C. I and III only

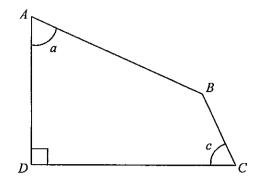
D. II and III only



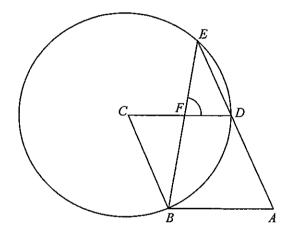
- 20. In the figure, ABCD, CDEF and EFGH are squares. AG cuts CD and EF at P and Q respectively. Find the ratio of the area of quadrilateral DEQP to the area of quadrilateral ABCP.
 - A. 1:2
 - B. 2:3
 - C. 3:5
 - D. 4:9



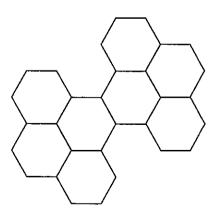
- 21. In the figure, AD =
 - A. $AB\cos a + BC\cos c$.
 - B. $AB\cos a + BC\sin c$.
 - C. $AB \sin a + BC \cos c$.
 - D. $AB \sin a + BC \sin c$.



- 22. In the figure, ABCD is a rhombus. C is the centre of the circle BDE and ADE is a straight line. BE and CD intersect at F. If $\angle ADC = 118^{\circ}$, then $\angle DFE =$
 - A. 59°.
 - B. 62°.
 - C. 78°.
 - D. 87°.



- 23. The figure below consists of eight identical regular hexagons. The number of axes of reflectional symmetry of the figure is
 - A. 2.
 - B. 4.
 - C. 6.
 - D. 8.



- 24. If the sum of the interior angles of a regular *n*-sided polygon is 3 240°, which of the following is true?
 - A. The value of n is 16.
 - B. Each exterior angle of the polygon is 18°.
 - C. The number of diagonals of the polygon is 20.
 - D. Each interior angle of the polygon is 160°.
- 25. If the straight lines hx + ky + 15 = 0 and 4x + 3y 5 = 0 are perpendicular to each other and intersect at a point on the x-axis, then k =
 - A. -12.
 - B. -4.
 - C. 3.
 - D. 16.
- 26. The coordinates of the points A and B are (9, -2) and (-1, 8) respectively. If C is a point lying on the straight line x-2y=0 such that AC=BC, then the x-coordinate of C is
 - A. 1.
 - B. 2.
 - C. 3°.
 - D. 4.
- 27. The equation of the circle C is $3x^2 + 3y^2 12x + 30y + 65 = 0$. Which of the following are true?
 - I. The radius of C is 14.
 - II. The origin lies outside C.
 - III. The coordinates of the centre of C are (2, -5).
 - A. I and II only
 - B. I and III only
 - C. II and III only
 - D. I, II and III

28.	Christine has one	\$1	coin,	one	\$2	coin,	one	\$5	coin and one	\$10	coin in her pocket.	If Christine
	takes out three coins randomly from her pocket, find the probability that she gets at least $$13$.											

- A. $\frac{1}{2}$
- B. $\frac{1}{4}$
- C. $\frac{3}{4}$
- D. $\frac{23}{24}$
- 29. A bag contains 1 red ball, 3 yellow balls and 6 white balls. In a lucky draw, a ball is randomly drawn from the bag and a certain number of tokens will be got according to the following table:

Colour of the ball drawn	Red	Yellow	White
Number of tokens got	90	20	10

Find the expected number of tokens got in the lucky draw.

- A. 10
- B. 21
- C. 40
- D. 61

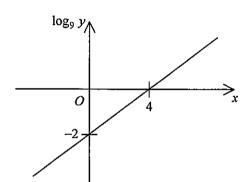
32 68 79 86 88 98 98 *a b c*

If the mean and the mode of the above data are 77 and 68 respectively, then the median of the above data is

- A. 76.
- B. 82.
- C. 85.
- D. 93.

Section B

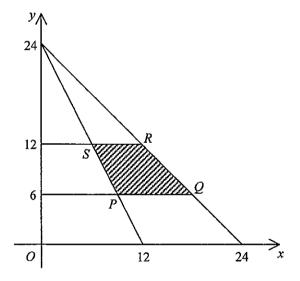
- 31. The L.C.M. of $9a^2b$, $12a^4b^3$ and $15a^6$ is
 - A. $3a^2$.
 - B. $3a^2b$.
 - C. $180a^6b^3$.
 - D. $180a^{12}b^4$.
- 32. The graph in the figure shows the linear relation between x and $\log_9 y$. If $y = ab^x$, then b =
 - A. -2.
 - B. $\frac{1}{81}$.
 - C. $\frac{1}{2}$
 - D. 3.



- 33. $BC000DE000000_{16} =$
 - A. $188 \times 16^{11} + 222 \times 16^6$.
 - B. $205 \times 16^{11} + 239 \times 16^6$.
 - C. $188 \times 16^{12} + 222 \times 16^7$.
 - D. $205 \times 16^{12} + 239 \times 16^7$.

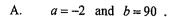
- 34. Let $u = \frac{7}{a+i}$ and $v = \frac{7}{a-i}$, where a is a real number. Which of the following must be true?
 - I. uv is a rational number.
 - II. The real part of u is equal to the real part of v.
 - III. The imaginary part of $\frac{1}{u}$ is equal to the imaginary part of $\frac{1}{v}$.
 - A. I only
 - B. II only
 - C. I and III only
 - D. II and III only
- 35. In the figure, PQ and SR are parallel to the x-axis. If (x, y) is a point lying in the shaded region PQRS (including the boundary), at which point does 7y-5x+3 attain its greatest value?





- 36. Let a_n be the *n*th term of a geometric sequence. If $a_3 = 21$ and $a_7 = 189$, which of the following must be true?
 - I. The common ratio of the sequence is less than 1.
 - II. Some of the terms of the sequence are irrational numbers.
 - III. The sum of the first 99 terms of the sequence is greater than 3×10^{24} .
 - A. I only
 - B. II only
 - C. I and III only
 - D. II and III only

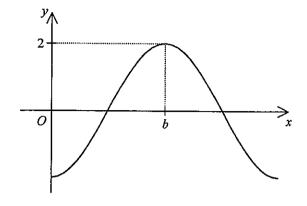
37. Let a and b be constants. If the figure shows the graph of $y = a \cos 2x^{\circ}$, then



B.
$$a = -2$$
 and $b = 360$.

C.
$$a = 2$$
 and $b = 90$.

D.
$$a = 2$$
 and $b = 360$.



38. For $0^{\circ} \le \theta \le 360^{\circ}$, how many roots does the equation $5\sin^2\theta + \sin\theta - 4 = 0$ have?

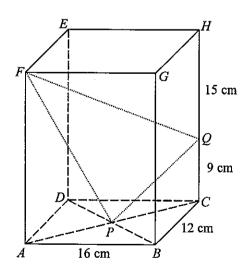
39. In the figure, ABCDEFGH is a rectangular block. AC and BD intersect at P. Q is a point lying on CH such that CQ = 9 cm and QH = 15 cm. Find $\sin \angle PFQ$.

A.
$$\frac{33}{65}$$

B.
$$\frac{56}{65}$$

C.
$$\frac{13}{5\sqrt{181}}$$

D.
$$\frac{58}{13\sqrt{181}}$$



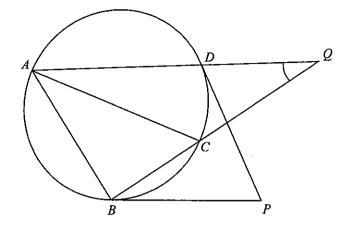
40. In the figure, AC is a diameter of the circle ABCD. PB and PD are tangents to the circle. AD produced and BC produced meet at Q. If $\angle BPD = 68^{\circ}$, then $\angle AQB =$





C. 32°.

D. 34°.



41. The straight line 2x-y-6=0 and the circle $x^2+y^2-8y-14=0$ intersect at P and Q. Find the y-coordinate of the mid-point of PQ.

A. –4

B. -2

C. 2

D. 4

42. There are 9 cans of coffee and 3 cans of tea in a box. If 4 cans are randomly chosen from the box, find the probability that at least 2 cans of tea are chosen.

A.
$$\frac{13}{55}$$

B.
$$\frac{21}{55}$$

C.
$$\frac{34}{55}$$

D.
$$\frac{42}{55}$$

43.		boys and 15 girls in a class. If 6 students are selected from the class to form a committee at most 2 girls, how many different committees can be formed?
	A.	271320
	В.	324 415

44. The stem-and-leaf diagram below shows the distribution of the scores (in marks) of a group of students in a test. Ada gets the highest score in the test.

Stem (tens)	Leaf (units)							
4	5	6	7	8				
5	5	5	6	8				
6	3	5	5	6	9	9		
7	0	0	1					
8	0	2	5					

Which of the following is/are true?

- I. The upper quartile of the distribution is 55 marks.
- II. The standard score of Ada in the test is lower than 2.
- III. The standard deviation of the distribution is greater than 12 marks.
 - A. I only
 - B. II only
 - C. I and III only
 - D. II and III only
- 45. The variance of a set of numbers is 49. Each number of the set is multiplied by 4 and then 9 is added to each resulting number to form a new set of numbers. Find the variance of the new set of numbers.
 - A. 196
 - B. 205
 - C. 784
 - D. 793

END OF PAPER

15

