

Set 1 – Full Solution

Paper 2

1. D	10. B	19. B	28. D	37. C
2. B	11. B	20. D	29. B	38. D
3. C	12. D	21. A	30. B	39. C
4. C	13. A	22. D	31. B	40. D
5. B	14. C	23. B	32. A	41. B
6. A	15. C	24. C	33. A	42. B
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8. B	17. C	26. D	35. D	44. C
9. C	18. C	27. A	36. D	45. D

1. D

$$\frac{(3y^2)^4}{9y}$$

$$= \frac{3^4 y^{2 \times 4}}{3^2 y}$$

$$= 3^{4-2} y^{8-1}$$

$$= 3^2 y^7$$

$$= 9y^7$$

2. B

$$4a = \frac{1}{5}(2c - 3ab)$$

$$20a = 2c - 3ab$$

$$3ab + 20a = 2c$$

$$a(3b + 20) = 2c$$

$$a = \frac{2c}{3b + 20}$$

3. C

$$ad - ae - bd + be + cd - ce$$

$$= ad - bd + cd - ae + be - ce$$

$$= d(a - b + c) - e(a - b + c)$$

$$= (a - b + c)(d - e)$$

4. C

Method 1

$$2(x^2 + 2a) = (x + 3)(2x + b) + 6$$

$$2x^2 + 4a = 2x^2 + 6x + bx + 3b + 6$$

$$2x^2 + 4a = 2x^2 + (6 + b)x + (3b + 6)$$

Comparing the coefficients of like terms,

$$0 = 6 + b$$

$$b = -6$$

$$4a = 3(-6) + 6$$

$$a = -3$$

Method 2

When $x = -3$,

$$2[(-3)^2 + 2a] = 6$$

$$a = -3$$

5. B

$f(x)$ is divisible by $x - 1$.

$$\therefore f(1) = 1 + k^2 - 6k + 8 = 0$$

$$k^2 - 6k + 9 = 0$$

$$k = 3$$

$$\therefore f(x) = x^3 + 9x^2 - 18x + 8$$

$$f(-2) = -60$$

6. A

A ✓ $0.08306 = 0.1$ (correct to 1 decimal place)
 B ✗ $0.08306 = 0.083$ (correct to 2 significant figures)
 C ✗ $0.08306 = 0.0831$ (correct to 3 significant figures)
 D ✗ $0.08306 = 0.0831$ (correct to 4 decimal places)

7. C

$$(x - 2s - 2)^2 = 9(s + 1)^2$$

$$x - 2s - 2 = 3(s + 1) \quad \text{or} \quad x - 2s - 2 = -3(s + 1)$$

$$x = 5s + 5 \quad \text{or} \quad x = -s - 1$$

8. B

- I. ✓ The graph opens downwards.
 II. ✓ The vertex of graph lies on the left of the y -axis.
 III. ✗ The vertex of graph lies above the x -axis.

9. C

$$2x - 7 > 3x + 2$$

$$-x > 9$$

$$x < -9$$

$$-3x + 5 > -4$$

$$-3x > -9$$

$$x < 3$$

\therefore Combining, $x < 3$.

10. B

Let $\$x$ and $\$y$ be the price of one pen and the price of one pencil respectively. The price of one notebook would then be $\$(x + y)$.

$$2y = (1 + 12.5\%)x$$

$$y = \frac{9}{16}x$$

The price of one notebook = $\$(x + \frac{9}{16}x) = \$(\frac{25}{16}x)$

The price of one notebook is $\frac{\frac{25}{16}x - x}{x} \times 100\% = 56.25\%$ higher than the price of one pen.

11. B

The amount

$$= 7000 \times \left(1 + \frac{0.09}{4}\right)^4$$

$$= \$7651.583232$$

The interest

$$= \$7651.583232 - \$7000$$

$$= \$651.583232$$

$$= \$652$$

12. D

$$\begin{aligned} (j+k) &: (i+k) \\ &= \left(3i + \frac{6i}{8}\right) : \left(i + \frac{6i}{8}\right) \\ &= \frac{15}{4}i : \frac{7}{4}i \\ &= 15 : 7 \end{aligned}$$

13. A

The actual area of the reservoir

$$\begin{aligned} &= 188 \times 20000^2 \\ &= 7.52 \times 10^{10} \text{ cm}^2 \\ &= 7.52 \times 10^6 \text{ m}^2 \\ &= 7.52 \text{ km}^2 \end{aligned}$$

14. C

The n th pattern has $1 + 3 + 5 + \dots + (2n-1)$ dots.
The number of dots in the 11th pattern = $1 + 3 + 5 + \dots + 21 = 121$

15. C

Let $z = k_1x^2 + \frac{k_2}{y^3}$, where k_1 and k_2 are non-zero constants.

$$\begin{cases} -62 = k_1(2)^2 + \frac{k_2}{1^3} \\ 24 = k_1(8)^2 + \frac{k_2}{2^3} \end{cases}$$

Solving, we have $k_1 = \frac{1}{2}$, $k_2 = -64$.

$$\therefore \frac{1}{2}(2)^2 - \frac{64}{(-4)^3} = 3$$

16. B

$$\frac{16350}{84} = 194.64 \text{ mL}$$

\therefore The minimum volume of orange juice = 194.64 mL.

17. C

Method 1

Let O be the centre of the circle $ABCD$, and M be the mid-point of AB .
 $OM \perp AB$

$$\sin \angle AOM = \frac{AM}{AO} = \frac{3}{4}$$

$$\angle AOB = 2\angle AOM = 2\sin^{-1} \frac{3}{4}$$

$$OM^2 = OA^2 - AM^2 = 4^2 - 3^2$$

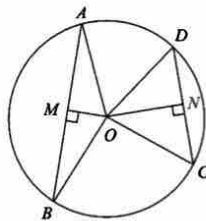
$$OM = \sqrt{7}$$

$$\text{The area of } \triangle OAB = \frac{1}{2} AB \times OM = \frac{1}{2} (6)(\sqrt{7}) = 3\sqrt{7}$$

$$\text{The area of the sector } OAB = \pi(4)^2 \frac{2\sin^{-1} \frac{3}{4}}{360^\circ} = 13.5690$$

$$OD = OC = 4 = CD$$

$$\therefore \angle COD = 60^\circ$$



Let N be the mid-point of CD .

$ON \perp CD$

$$ON^2 = OD^2 - DN^2 = 4^2 - 2^2$$

$$ON = 2\sqrt{3}$$

$$\text{The area of } \triangle OCD = \frac{1}{2} CD \times ON = \frac{1}{2} (4)(2\sqrt{3}) = 4\sqrt{3}$$

$$\text{The area of the sector } OCD = \pi(4)^2 \frac{60^\circ}{360^\circ} = \frac{8}{3}\pi$$

The area of the shaded region

$$= \text{Area of the circle} - \text{Area of the sector } OAB + \text{Area of } \triangle OAB - \text{Area of the sector } OCD + \text{Area of } \triangle OCD$$

$$= \pi(4)^2 - 13.5690 + 3\sqrt{7} - \frac{8}{3}\pi + 4\sqrt{3}$$

$$= 43.2 \text{ cm}^2 \text{ (corr. to 3 sig. fig.)}$$

Method 2

Let O be the centre of the circle $ABCD$.

$$\text{In } \triangle OAB, \text{ by cosine formula, } \cos \angle AOB = \frac{OA^2 + OB^2 - AB^2}{2(OA)(OB)} = \frac{4^2 + 4^2 - 6^2}{2(4)(4)} = \frac{-1}{8}$$

$$\text{The area of } \triangle OAB = \frac{1}{2} (OA)(OB) \sin \angle AOB = \frac{1}{2} (4)(4) \sin \left(\cos^{-1} \frac{-1}{8} \right) = 7.93725$$

$$\text{The area of the sector } OAB = \pi(4)^2 \frac{\cos^{-1} \frac{-1}{8}}{360^\circ} = 13.5690$$

$$OD = OC = 4 = CD$$

$$\therefore \angle COD = 60^\circ$$

$$\text{The area of } \triangle OCD = \frac{1}{2} (OC)(OD) \sin \angle COD = \frac{1}{2} (4)(4) \sin 60^\circ = 4\sqrt{3}$$

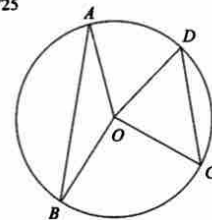
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The area of the shaded region

$$= \text{Area of the circle} - \text{Area of the sector } OAB + \text{Area of } \triangle OAB - \text{Area of the sector } OCD + \text{Area of } \triangle OCD$$

$$= \pi(4)^2 - 13.5690 + 7.93725 - \frac{8}{3}\pi + 4\sqrt{3}$$

$$= 43.2 \text{ cm}^2 \text{ (corr. to 3 sig. fig.)}$$



18. C

Method 1

Produce BE and AD to meet at F .

Since $BC \parallel AF$, $\triangle BCE \sim \triangle FDE$ (AAA).

$BE : FE = BC : FD = CE : DE = 3 : 1$ (corr. sides, $\sim \Delta$ s)

As $BE : EF = 3 : 1$, Area of $\triangle ABE : \text{Area of } \triangle AEF = 3 : 1$.

The area of $\triangle AEF = 2 \text{ cm}^2$

As $BC : FD = 3 : 1$, and $BC : AD = 2 : 1$, $AD : DF = 3 : 2$.

Area of $\triangle ADE : \text{Area of } \triangle FDE = 3 : 2$

Area of $\triangle ADE + \text{Area of } \triangle FDE = \text{Area of } \triangle AEF = 2 \text{ cm}^2$

$$\therefore \text{The area of } \triangle ADE = 2 \times \frac{3}{2+3} = 1.2 \text{ cm}^2$$

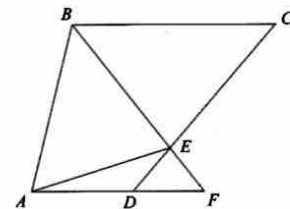
The area of $\triangle FDE = 2 - 1.2 = 0.8 \text{ cm}^2$

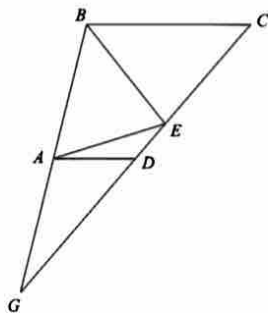
Since $\triangle BCE \sim \triangle FDE$ with side ratio $3 : 1$,

Area of $\triangle BCE : \text{Area of } \triangle FDE = 3^2 : 1^2 = 9 : 1$.

The area of $\triangle BCE = 9(0.8) = 7.2 \text{ cm}^2$

The area of the trapezium $ABCD = 6 + 1.2 + 7.2 = 14.4 \text{ cm}^2$



Method 2Produce BA and CD to meet at G .Since $BC \parallel AD$, $\triangle BCG \sim \triangle ADG$ (AAA). $CG : DG = BG : AG = BC : AD = 2 : 1$ (corr. sides, $\sim \Delta$ s) $\therefore AB = AG$ and $CD = DG$ Area of $\triangle AEG =$ Area of $\triangle ABE = 6 \text{ cm}^2$ Since $CD = DG$ and $CE : DE = 3 : 1$, $GD : DE : EC = 4 : 1 : 3$, $CG : EG = 8 : 5$.Area of $\triangle GBC$: Area of $\triangle BEG = 8 : 5$ The area of $\triangle GBC = (6+6) \times \frac{8}{5} = 19.2 \text{ cm}^2$ Since $\triangle BCG \sim \triangle ADG$ with side ratio $2 : 1$,Area of $\triangle BCG$: Area of $\triangle ADG = 2^2 : 1^2 = 4 : 1$.The area of $\triangle ADG = 19.2 \times \frac{1}{4} = 4.8 \text{ cm}^2$ The area of trapezium $ABCD = 19.2 - 4.8 = 14.4 \text{ cm}^2$ 

19. B

Let h be the height of the cone.

$$4\pi r^2 = \pi r \sqrt{r^2 + h^2}$$

$$4r = \sqrt{r^2 + h^2}$$

$$16r^2 = r^2 + h^2$$

$$h^2 = 15r^2$$

$$h = \sqrt{15}r$$

$$\therefore \text{The volume of the cone} = \frac{1}{3}\pi r^2 h = \frac{1}{3}\pi r^2(\sqrt{15}r) = \frac{\sqrt{15}}{3}\pi r^3$$

20. D

I. ✓

$$\tan(180^\circ - \theta) = -\tan \theta$$

$$\therefore \tan \theta + \tan(180^\circ - \theta) = \tan \theta - \tan \theta = 0$$

II. ✓

$$\sin x > 0 \text{ for } 0^\circ < x < 180^\circ.$$

$$\therefore \sin \theta > 0$$

$$\text{Since } 60^\circ < (150^\circ - \theta) < 150^\circ,$$

$$\therefore \sin(150^\circ - \theta) > 0$$

$$\frac{\sin \theta}{\sin(150^\circ - \theta)} > 0$$

III. ✓

$$\cos x < 0 \text{ for } 90^\circ < x < 270^\circ.$$

$$\text{Since } 120^\circ < (\theta + 120^\circ) < 210^\circ,$$

$$\therefore \cos(\theta + 120^\circ) < 0$$

$$\cos x > 0 \text{ for } -90^\circ < x < 90^\circ.$$

$$\text{Since } -90^\circ < (\theta - 90^\circ) < 0^\circ$$

$$\therefore \cos(\theta - 90^\circ) > 0$$

$$\cos(\theta + 120^\circ) - \cos(\theta - 90^\circ) < 0$$

21. A

$$\angle BAD = \angle BDA = 47^\circ \text{ (base } \angle\text{s, isos. } \Delta)$$

$$\angle DAC = \angle BDA - \angle DCA \text{ (ext. } \angle \text{ of } \Delta)$$

$$= 47^\circ - 26^\circ$$

$$= 21^\circ$$

$$\angle ABE = \angle BAC \text{ (alt. } \angle\text{s, } EB \parallel AC)$$

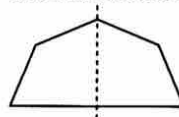
$$= 47^\circ + 21^\circ$$

$$= 68^\circ$$

22. D

I. ✓ The sum of the interior angles $= 180^\circ \times (5 - 2) = 540^\circ$ II. ✓ The sum of the exterior angles of a polygon is 360° .

III. ✓



23. B

$$OB = OC$$

$$\therefore \angle OCB = \frac{180^\circ - 36^\circ}{2} = 72^\circ$$

$$\angle BAC = 18^\circ \text{ (} \angle \text{ at centre twice } \angle \text{ at circumference)}$$

$$\angle BCA = 2 \times \angle BAC = 36^\circ \text{ (arcs prop. to } \angle\text{s at circumference)}$$

$$\therefore \angle OCA = 72^\circ - 36^\circ = 36^\circ$$

24. C

12 pentagons have $12 \times 5 = 60$ sides.20 hexagons have $20 \times 6 = 120$ sides.Each edge is the side of two faces, so there are $\frac{60+120}{2} = 90$ edges.By Euler's formula, $V + F - E = 2$.

$$V = 2 - 32 + 90 = 60$$

 \therefore The polyhedron has 90 edges and 60 vertices.

25. B

The coordinates of B are $(6, 7)$.The coordinates of the reflection image of B with respect to the y -axis are $(-6, 7)$.

26. D

The slope of $L_1 = \tan 135^\circ = -1$ The equation of L_1 is

$$y = -x + 5 \dots\dots (1)$$

The equation of L_2 is

$$\frac{x}{-3} + \frac{y}{1} = 1$$

$$y = \frac{x}{3} + 1 \dots\dots (2)$$

Solving, we have $x = 3$ and $y = 2$.

27. A
The coordinates of the centre are $(-h, -k)$.
From the figure,

I. ✓
 $-h > 0$
 $\therefore h < 0$
 $-k < 0$
 $\therefore k > 0$
 $hk < 0$

II. ✓

The x-coordinate of the centre $< r$

$-h < r$

$h > -r$

III. ✗

The y-coordinate of the centre $< -r$

$-k < -r$

$k > r$

28. D
I. ✗

Since the range is 10, $4 \leq p \leq 14$ and $4 \leq q \leq 14$.

Since the median is 7, one is smaller than or equal to 7 and another is greater than or equal to 7.

Since $p < q$, $4 \leq p \leq 7$.

p can be equal to 4.

II. ✓

Since $p < q$, $4 \leq p \leq 7$ and $7 \leq q \leq 14$.

III. ✓

If mean = 7.8 and $q = 7$, then $p = 7$. It is impossible.

29. B
I. ✗ 40 is the median, the mean cannot be determined from the diagram.
II. ✗ The inter-quartile range is 20 lessons/15 hours.
III. ✓ 54 hours is longer than the duration of 70 lessons.

30. B
The standard deviation = 1.40248 = 1.40

31. B
 $m^2 - 16 = (m+4)(m-4)$
 $m^2 + 8m + 16 = (m+4)^2$
 $m^3 - 64 = (m-4)(m^2 + 4m + 16)$
 \therefore The L.C.M. = $(m+4)^2(m-4)(m^2 + 4m + 16)$

32. A
Method 1
Since the graph is downward sloping, $0 < a < 1$.

Put $x = 1$, $y = \log_a(1) + b = b$

Note that when $x > \frac{1}{2}$, $y < 0$.

$\therefore b < 0$

Method 2

$$y = \log_a x + b = \frac{\log x}{\log a} + b$$

Consider the graph of $y = \log x$ in the figure.

Since the graphs are in opposite direction, $\frac{1}{\log a}$ is negative.

$\therefore \log a$ is negative, so $0 < a < 1$.

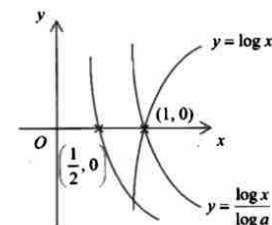
Consider the graph of $y = \frac{\log x}{\log a}$ in the figure.

For $y = 0$, $x = 1$. So it still passes through the point $(1, 0)$.

However, for $y = \frac{\log x}{\log a} + b$, it passes through the point $(\frac{1}{2}, 0)$.

so the graph is shifted downwards.

$\therefore b < 0$



33. A
 10001100011_2
 $= 2^{10} + 2^6 + 2^2 + 2 + 1$
 $= 2^{10} + 99$

34. B
Method 1
 $\alpha + \beta = -6$ and $\alpha\beta = 12$
 $\alpha^4 + \beta^4$
 $= \alpha^4 + 2\alpha^2\beta^2 + \beta^4 - 2\alpha^2\beta^2$
 $= (\alpha^2 + \beta^2)^2 - 2\alpha^2\beta^2$
 $= (\alpha^2 + 2\alpha\beta + \beta^2 - 2\alpha\beta)^2 - 2\alpha^2\beta^2$
 $= [(\alpha + \beta)^2 - 2\alpha\beta]^2 - 2(\alpha\beta)^2$
 $= [(-6)^2 - 2(12)]^2 - 2(12)^2$
 $= -144$

Method 2

$\alpha + \beta = -6$

$x^2 + 6x + 12 = 0$

$\alpha^2 = -6\alpha - 12$ and $\beta^2 = -6\beta - 12$

$\alpha^4 = (-6\alpha - 12)^2 = 36(\alpha^2 + 4\alpha + 4) = 36(-6\alpha - 12 + 4\alpha + 4) = 36(-2\alpha - 8) = -72(\alpha + 4)$

Similarly, $\beta^4 = -72(\beta + 4)$.

$\therefore \alpha^4 + \beta^4 = [-72(\alpha + 4)] + [-72(\beta + 4)] = -72(\alpha + \beta + 8) = -72(-6 + 8) = -144$

35. D
 $\frac{2i - \alpha}{3i - 1}$
 $= \frac{2i - \alpha}{3i - 1} \times \frac{-3i - 1}{-3i - 1}$
 $= \frac{6 - 2i + 3\alpha i + \alpha}{9 + 1}$
 $= \frac{6 + \alpha}{10} + \frac{3\alpha - 2}{10}i$

36. D

$$f(x) = g(x)$$

$$-x^2 + bx + c = mx + c$$

$$x^2 + (m-b)x = 0$$

Let α and β be the roots of the equation $x^2 + (m-b)x = 0$.

$$\alpha + \beta = -(m-b) = b-m$$

$$\alpha\beta = 0$$

The distance between A and B

$$= \sqrt{(\alpha - \beta)^2 + [(m\alpha + c) - (m\beta + c)]^2}$$

$$= \sqrt{(\alpha - \beta)^2 + m^2(\alpha - \beta)^2}$$

$$= \sqrt{(1+m^2)(\alpha - \beta)^2}$$

$$= \sqrt{(1+m^2)[(\alpha + \beta)^2 - 4\alpha\beta]}$$

$$= \sqrt{(1+m^2)(b-m)^2}$$

$$= (m-b)\sqrt{1+m^2} \text{ or } -(m-b)\sqrt{1+m^2} \text{ (rejected)}$$

37. C

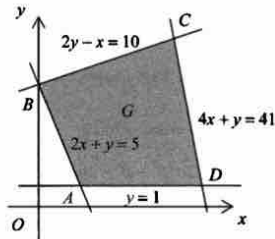
With the illustration of the graph on the right,

G is the shaded region, with vertices A, B, C and D .

After solving the equations, the coordinates of A, B, C and D are $(2, 1), (0, 5), (8, 9)$ and $(10, 1)$ respectively.

The value of $75 - 4x - 3y$ at A, B, C and D are 64, 60, 16 and 32 respectively.

\therefore The maximum value of $75 - 4x - 3y$ is 64.



38. D

The n th term

= Sum of the first n th terms - Sum of the first $(n-1)$ th terms

$$= 2n(n-9) - 2(n-1)(n-1-9)$$

$$= 2(n^2 - 9n) - 2(n^2 - 11n + 10)$$

$$= 4n - 20$$

$$I. \quad \times$$

$$4n - 20 < 0$$

$$n < 5$$

\therefore Only the first 4 terms are negative.

Sum of all negative terms = $2(4)(4-9) = -40$

II. \checkmark

$$\text{The 2nd term} = 4(2) - 20 = -12$$

$$\text{The 9th term} = 4(9) - 20 = 16$$

$$16 - (-12) = 28$$

III. \checkmark

$$\text{The } n\text{th term} = 4n - 20 = 4(n-5)$$

Since n is an integer, $n-5$ is also an integer.

\therefore All terms are divisible by 4.

39. C

The graph is sinusoidal.

Let the equation be $y = a \sin(hx^\circ + k) + b$.

Since the amplitude is 2, $a = 2$.

The range of y is from -3 to 1 , where the range of $y = 2 \sin(x^\circ)$ is from -2 to 2 .

Thus, the graph is shifted downwards by 1 unit.

$$b = -1$$

When $x = 0$ or $x = 1440$, $y = 0$.

$$0 = 2 \sin(k) - 1$$

$$\sin k = 0.5$$

From the choices, $k = 30^\circ$.

$$0 = 2 \sin(1440h^\circ + 30^\circ) - 1$$

$$\sin(1440h^\circ + 30^\circ) = 0.5$$

$$1440h^\circ + 30^\circ = 30^\circ \text{ or } 150^\circ \text{ or } 390^\circ \text{ or } 510^\circ \text{ or } 750^\circ \text{ or } \dots$$

$$1440h^\circ = 0^\circ \text{ or } 120^\circ \text{ or } 360^\circ \text{ or } 480^\circ \text{ or } 720^\circ \text{ or } \dots$$

$$h = 0 \text{ (rejected) or } \frac{1}{12} \text{ or } \frac{1}{4} \text{ or } \frac{1}{3} \text{ or } \frac{1}{2} \text{ or } \dots$$

Since there are three x -intercepts within $0 < x \leq 1440$, the third root of h should be chosen.

$$\therefore h = \frac{1}{3}$$

Thus, the graph can represent the equation $y = 2 \sin\left(\frac{x^\circ}{3} + 30^\circ\right) - 1$.

40. D

I. \checkmark

$BCDE$ is a square.

$$BD = \sqrt{1^2 + 1^2} = \sqrt{2} \text{ cm}$$

$\triangle ABC$ is equilateral.

Let M be a point on AC such that $BM \perp AC$.

$$BM = BC \sin 60^\circ = \frac{\sqrt{3}}{2} \text{ cm}$$

$$\text{By symmetry, } DM = \frac{\sqrt{3}}{2} \text{ cm.}$$

By cosine formula,

$$\cos \angle BMD = \frac{\left(\frac{\sqrt{3}}{2}\right)^2 + \left(\frac{\sqrt{3}}{2}\right)^2 - (\sqrt{2})^2}{2 \left(\frac{\sqrt{3}}{2}\right) \left(\frac{\sqrt{3}}{2}\right)} = -\frac{1}{3}$$

The angle between the plane ABC and the plane $ADC = \angle BMD = \cos^{-1}\left(-\frac{1}{3}\right)$

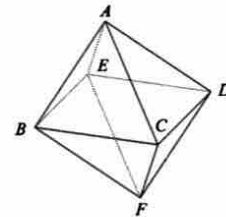
II. \checkmark

The surface area of the octahedron

$$= 8 \times \text{Area of } \triangle ABC$$

$$= 8 \left[\frac{1}{2} (1)(1) \sin 60^\circ \right]$$

$$= 2\sqrt{3} \text{ cm}^2$$



III. ✓

By symmetry, $AF = BD = \sqrt{2}$ cm.Let P be the intersection point of AF and the plane $BCDE$.By symmetry, $AP \perp$ the plane $BCDE$ and $AP = \frac{1}{2}AF = \frac{\sqrt{2}}{2}$ cm.By symmetry, the pyramid $ABCDE$ and the pyramid $FBCDE$ are congruent.

The volume of the octahedron

 $= 2 \times$ Volume of pyramid $ABCDE$

$$= 2 \times \left(\frac{1}{3} \times 1^2 \times \frac{\sqrt{2}}{2} \right)$$

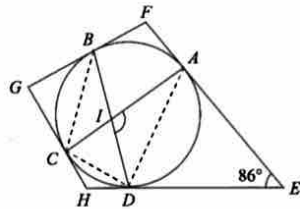
$$= \frac{\sqrt{2}}{3} \text{ cm}^3$$

41. B

Join AD , BC and CD . $\angle FGH = 180^\circ - 86^\circ = 94^\circ$ (opp. \angle s, cyclic quad.) $AE = DE$ and $BG = CG$ (tangent properties)

$$\angle ADE = \frac{180^\circ - 86^\circ}{2} = 47^\circ$$

$$\angle BCG = \frac{180^\circ - 94^\circ}{2} = 43^\circ$$

 $\angle ACD = 47^\circ$ and $\angle BDC = 43^\circ$ (\angle in alt. segment) $\angle AID = \angle ACD + \angle BDC = 47^\circ + 43^\circ = 90^\circ$ (ext. \angle of Δ)

42. B

A ✗

Put $y = 4x + 3$ into $x^2 + y^2 + x + 4y - 2 = 0$,

$$x^2 + (4x + 3)^2 + x + 4(4x + 3) - 2 = 0$$

$$17x^2 + 41x + 19 = 0$$

$$\Delta = (41)^2 - 4(17)(19) = 389 > 0$$

 \therefore The straight line and the circle intersect at two distinct points.

B ✓

Put $y = 4x + 3$ into $x^2 + y^2 - 4x + y + 2 = 0$,

$$x^2 + (4x + 3)^2 - 4x + (4x + 3) + 2 = 0$$

$$17x^2 + 24x + 14 = 0$$

$$\Delta = (24)^2 - 4(17)(14) = -376 < 0$$

 \therefore The straight line and the circle do not intersect.

C ✗

Put $y = 4x + 3$ into $x^2 + y^2 + 3x + 4y - 3 = 0$,

$$x^2 + (4x + 3)^2 + 3x + 4(4x + 3) - 3 = 0$$

$$17x^2 + 43x + 18 = 0$$

$$\Delta = (43)^2 - 4(17)(18) = 625 > 0$$

 \therefore The straight line and the circle intersect at two distinct points.

D ✗

Put $y = 4x + 3$ into $x^2 + y^2 + 4x - 7y + 12 = 0$,

$$x^2 + (4x + 3)^2 + 4x - 7(4x + 3) + 12 = 0$$

$$17x^2 = 0$$

$$\Delta = (0)^2 - 4(17)(0) = 0$$

 \therefore The straight line and the circle intersect at one point only.

43. B

The number of committees

$$= C_3^{4+12} - C_3^{12} - C_3^{14}$$

$$= 133146$$

44. C

Let x be John's score, z be John's standard score, μ be the mean and σ be the standard deviation.

$$z = \frac{x - \mu}{\sigma}$$

$$\frac{196 - 136}{54} < z < \frac{200 - 119}{54}$$

$$1.11111 < z < 1.5$$

45. D

By observation:

$$2a + 2 = 2(a + 7) - 12$$

$$4b - 12 = 2(2b) - 12$$

$$2c - 22 = 2(c - 5) - 12$$

$$8 = 2(10) - 12$$

Each of the original data is multiplied by 2 and then 12 is subtracted from it.

Therefore, the variance is multiplied by $2^2 = 4$.The required variance $= 4(18) = 72$