

**Final Examination 2021 – 2022**  
**Mathematics Compulsory Part**  
**Paper 2**

Form Six

Name: \_\_\_\_\_  
Class: \_\_\_\_\_ ( )

- Time allowed : 1 hour and 15 minutes
- Answer ALL questions. All the answers must be marked on the MC answer sheet with pencil or marks will be deducted.
- The diagrams are not necessarily drawn to scale.

**Section A**

1.  $\frac{(3^n)(4^n)}{6^{2n}} =$
- A. 1.  
B.  $\frac{1}{3^n}$ .  
C.  $\frac{1}{2^n}$ .  
D.  $2^n$ .
2.  $(a + b)^2(a - b) =$
- A.  $a^3 - a^2b - ab^2 - b^3$ .  
B.  $a^3 - a^2b + ab^2 - b^3$ .  
C.  $a^3 + a^2b - ab^2 - b^3$ .  
D.  $a^3 + a^2b + ab^2 - b^3$ .
3. If  $\frac{h}{h-k} = \frac{2}{2h+k}$ , then  $k =$
- A.  $\frac{2h(1-h)}{h+2}$ .  
B.  $\frac{2h(h-1)}{h+2}$ .  
C.  $\frac{2h(1+h)}{h-2}$ .  
D.  $\frac{2h(1+h)}{2-h}$ .
4. If  $0.054546 < x < 0.054553$ , which of the following is true?
- A.  $x = 0.0545$  (correct to 3 decimal places)  
B.  $x = 0.0545$  (correct to 3 significant figures)  
C.  $x = 0.05455$  (correct to 4 decimal places)  
D.  $x = 0.05455$  (correct to 4 significant figures)
5.  $\frac{9}{d-3} - \frac{8}{d+4} =$
- A.  $\frac{d-12}{(d-3)(d+4)}$ .  
B.  $\frac{d+1}{(d-3)(d+4)}$ .  
C.  $\frac{d+12}{(d-3)(d+4)}$ .  
D.  $\frac{d+60}{(d-3)(d+4)}$ .
6. If  $a$  and  $b$  are constants such that  $(2x-a)^2 + 4 \equiv 4(x-2)(x-1) + b$ , then  $b =$
- A. -11.  
B. -5.  
C. 5.  
D. 11.
7. Let  $g(x) = 4x^2 - 2x - 1$ . If  $g(3a) = 10a$ , find  $a$ .
- A.  $a = -\frac{1}{2}$  or  $\frac{1}{18}$   
B.  $a = -\frac{1}{3}$  or  $\frac{1}{12}$   
C.  $a = -\frac{1}{12}$  or  $\frac{1}{3}$   
D.  $a = -\frac{1}{18}$  or  $\frac{1}{2}$

8. Let  $f(x) = 2x^3 - ax + b$ ,  $x^2 - 4$  is a factor of  $f(x)$ . Find the remainder when  $f(x)$  is divided by  $x - 1$ .

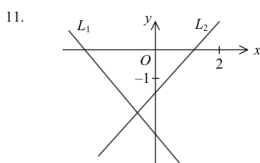
- A. -6
- B. -1
- C. 1
- D. 6

9. The base radius of a right circular cylinder is increased by 20%, while its height is decreased by  $p\%$ . If the volume of the cylinder is increased by 8%, find  $p$ .

- A. 10
- B. 20
- C. 25
- D. 31

10. If  $p$  and  $q$  are positive numbers such that  $\frac{p+q}{10p+2q} = \frac{q-p}{5p-q}$ , then  $p : q =$

- A. 1 : 3
- B. 3 : 5
- C. 5 : 3
- D. 3 : 1



11. In the figure, the equations of the straight lines  $L_1$  and  $L_2$  are  $ax + by - 2 = 0$  and  $px + 2y - q = 0$  respectively. Which of the following are true?

- I.  $b < 0$
- II.  $q < -2$
- III.  $2p + q > 0$

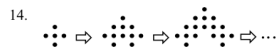
- A. I and II only
- B. I and III only
- C. II and III only
- D. I, II and III

12. Find the greatest integer satisfying  $\frac{3x}{2} + 18 < 1 - 3x$  or  $5 - 2x > 16$ .

- A. -3
- B. -4
- C. -5
- D. -6

13. If  $r$  varies directly as the square root of  $s$  and inversely as the cube root of  $t$ , which of the following must be constant?

- A.  $\frac{s^3}{t^2r^6}$
- B.  $\frac{s^2}{t^3r^6}$
- C.  $\frac{s^3r^6}{t^3}$
- D.  $\frac{s^2r^6}{t^3}$



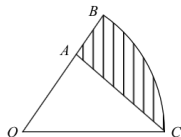
14. In the figure, the 1st pattern consists of 5 dots. For any positive integer  $n$ , the  $(n + 1)$ th pattern is formed by adding 6 dots to the  $n$ th pattern. Find the number of dots in the 8th pattern.

- A. 41
- B. 47
- C. 53
- D. 59

15. A frustum is made by cutting off the upper part of a right circular cone with base radius 42 cm. The radius of the top circular surface of the frustum is 24 cm. The volume of the frustum is  $8370\pi$  cm<sup>3</sup>. Find the height of the frustum.

- A. 6.1 cm
- B. 7.5 cm
- C. 10 cm
- D. 17.5 cm

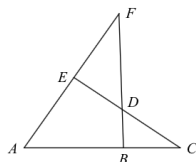
16.



In the figure,  $O$  is the centre of the sector  $OBC$ .  $A$  is a point on  $OB$ .  $OA = 10$  cm,  $OC = 17$  cm and  $AC = 9$  cm. Find the area of the shaded region correct to 3 significant figures.

- A.  $21.3 \text{ cm}^2$
- B.  $27.2 \text{ cm}^2$
- C.  $29.6 \text{ cm}^2$
- D.  $34.8 \text{ cm}^2$

17.



In the figure,  $ABC$  and  $AEF$  are straight lines.  $\triangle ABF \sim \triangle DBC$ .  $BF$  intersects  $CE$  at  $D$ .  $AF = 143$  cm,  $BD = 15$  cm and  $DF = 117$  cm. Find the area of  $\triangle DEF$ .

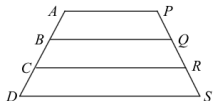
- A.  $2430 \text{ cm}^2$
- B.  $2852 \text{ cm}^2$
- C.  $2970 \text{ cm}^2$
- D.  $3630 \text{ cm}^2$

18.  $ABCDEF$  is a regular hexagon. Which of the following are true?

- I.  $\angle ACB = 30^\circ$ .
- II.  $\triangle CFE \cong \triangle CFD$ .
- III.  $\triangle ACE$  is an equilateral triangle.

- A. I and II only
- B. I and III only
- C. II and III only
- D. I, II and III

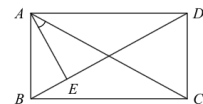
19.



In the figure,  $ABCD$  and  $PQRS$  are straight lines.  $AB = BC = CD$  and  $AP \parallel BQ \parallel CR \parallel DS$ .  $AP = 8$  cm and  $DS = 12$  cm. Find the ratio of the area of  $BCRQ$  to the area of  $ADSP$ .

- A.  $1 : 6$
- B.  $1 : 4$
- C.  $1 : 3$
- D.  $1 : 2$

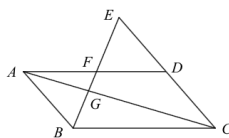
20.



$ABCD$  is a rectangle.  $E$  is a point on  $BD$  such that  $AE \perp BD$ . If  $\angle BDC = 76^\circ$ , find  $\angle CAE$ .

- A.  $14^\circ$
- B.  $38^\circ$
- C.  $52^\circ$
- D.  $62^\circ$

21.



In the figure,  $BE$  cuts  $AD$  and  $AC$  at  $F$  and  $G$  respectively.  $CDE$  is a straight line.  $AD \parallel BC$ . Suppose  $BG : GF : FE = 5 : 3 : 8$ . Find the ratio of the area of  $\triangle ABG$  to the area of  $\triangle DEF$ .

- A.  $3 : 4$
- B.  $15 : 16$
- C.  $45 : 46$
- D.  $1 : 1$