

**ST. STEPHEN'S GIRLS' COLLEGE**  
**Final Examination 2017 - 18**

**Form 6**

**LC, WMC, KAL, SCHL, CYN**

**126 students**

**Mathematics**  
**Paper I**  
**Time allowed : 2¼ hours**  
**Question/Answer Paper**

**Please read the following instructions very carefully.**

1. Write your class, class number, name and division (if applicable) in the spaces provided on this cover.
2. This paper consists of THREE sections, A(1), A(2) and B. Each section carries 35 marks.
3. Attempt ALL questions in this paper. Write your answers in the spaces provided in this Question/Answer Paper.
4. Graph paper and supplementary answer sheets will be supplied on request. Write your class, class number and name on each sheet, and fasten them with string **INSIDE** this paper.
5. Unless otherwise specified, all working must be clearly shown.
6. Unless otherwise specified, numerical answers should either be exact or correct to 3 significant figures.
7. The diagrams in this paper are not necessarily drawn to scale.

<b>Class</b>	
<b>Class No.</b>	
<b>Name</b>	
<b>Division</b>	

	<b>Marker's Use Only</b>
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<b>Total</b>	

SECTION A(1) (35 marks)

1. Make  $q$  the subject of the formula  $p = \frac{r - 2q}{q + r}$ . (3 marks)

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2. Simplify  $\frac{x^{-8}}{(x^2y^4)^{-3}}$  and express your answer with positive indices. (3 marks)

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3. Factorize  
(a)  $9a^2 - 6ab + b^2$  ,  
(b)  $9a^2 - 6ab + b^2 - 66a + 22b$  . (3 marks)

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4. The prices of an apple and an orange are \$3 and \$4.5 respectively. If Susan buys 25 of these fruits for \$90, find the number of oranges bought. (4 marks)

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5. (a) Solve the inequality  $2(x - 5) < 3x + 8$ .  
(b) Write down the least integer satisfying the inequality  $2(x - 5) < 3x + 8$ . (3 marks)

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**F.6**

**Mathematics Paper I (Final Examination 2017-18)**

6. In Figure 1, the coordinates of point  $A$  are  $(-2, 6)$ .  $B$  is the image of  $A$  after it has been reflected with respect to the  $y$ -axis and then translated 4 units downwards.

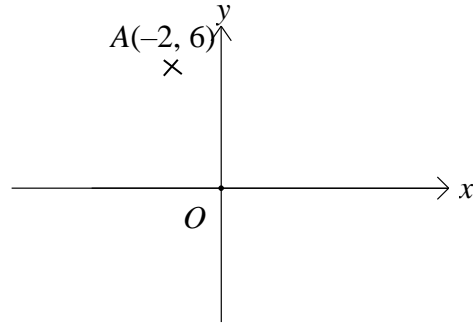


Figure 1

- (a) Write down the coordinates of  $B$ .
- (b) Is  $AB$  perpendicular to  $OB$ ? Explain your answer.
- (c) Find the area of  $\triangle OAB$ .

(5 marks)

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**F.6****Mathematics Paper I (Final Examination 2017-18)**

8. It is given that  $y$  varies inversely as the cube root of  $x$ . When  $x = 125$ ,  $y = 35$ .

- (a) Express  $y$  in terms of  $x$ .
- (b) If  $x$  is decreased by 27.1%, write down the percentage change of  $y$ .

(5 marks)

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9. Using an electronic balance, Peter finds that the weight of 50 identical paper clips is 79.0 g, correct to the nearest 0.1 g.

- (a) Estimate the weight of each paper clip.
- (b) Find the percentage error of the estimation in (a).
- (c) Write down the least possible weight of each paper clip.

(5 marks)

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**F.6**

**Mathematics Paper I (Final Examination 2017-18)**

11. The stem-and-leaf diagram below shows the distribution of a data set  $A$ . It is known that in the distribution of the data set  $A$ , the mean, the median and the mode are all equal.

**Distribution of data set  $A$**

<u>Stem (ten units)</u>	<u>Leaf (1 unit)</u>
0	1 4
1	0 1 $z$ 6 8
2	0 0 1 $x$ $x$ 2 3 9
3	3 7 8
4	3

- (a) Find  $x$  and  $z$ .
- (b) Find the range and the inter-quartile range.
- (c) It is given that the range of another data set  $B$  is 36 and the inter-quartile range of data set  $B$  is 16. Determine which data set is more dispersed.

(7 marks)

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**F.6**

**Mathematics Paper I (Final Examination 2017-18)**

13. In Figure 3,  $A(0, 4)$ ,  $B(6, 7)$  and  $C(0, -2)$  are three points on the rectangular coordinate plane.  $L$  is the perpendicular bisector of  $AB$  and it intersects  $AB$  at  $M$ .

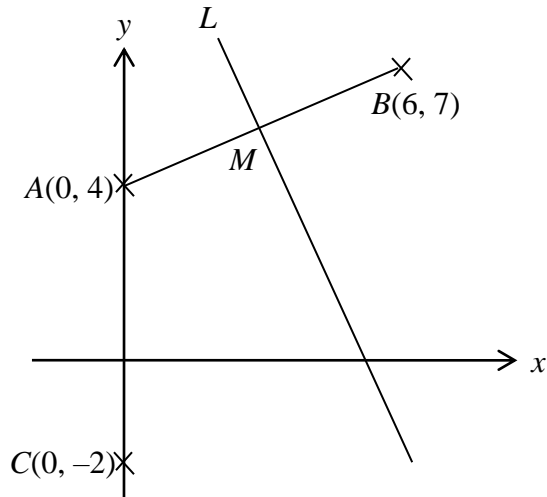


Figure 3

- (a) (i) Find the slope of  $AB$ .  
(ii) Hence, find the equation of  $L$ . (3 marks)
- (b)  $P$  is a point on the rectangular coordinate plane such that  $PA = PB = PC$ . Using (a)(ii), find the coordinates of  $P$ . (2 marks)
- (c) Let  $H$  be a moving point on the circle passing through  $A, B$  and  $C$ . Using (b), find the shortest possible distance between  $H$  and  $M$  correct to 2 decimal places. (2 marks)

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**SECTION B (35 marks)**

15. Let  $a$  and  $b$  be constants. Denote the graph of  $y = \log_a x + b$  by  $G$ . The  $x$ -intercept of  $G$  is 16 and  $G$  passes through the point  $(64, 2)$ . Express  $x$  in terms of  $y$ . (4 marks)

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16. A country adopts a plan to import crude oil from another country. It is given that the volume of crude oil imported in the 1st year since the start of the plan is  $8 \times 10^7 \text{ m}^3$  and in subsequent years, the volume of crude oil imported each year is 10% less than the volume of crude oil imported in the previous year.
- (a) Find the total volume of crude oil imported in the first 10 years since the start of the plan. (2 marks)
- (b) Find the least value of  $n$  such that the total volume of crude oil imported in the first  $n$  years since the start of the plan exceeds  $7 \times 10^8 \text{ m}^3$ . (2 marks)

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**F.6**

**Mathematics Paper I (Final Examination 2017-18)**

17. A jury of 5 is chosen at random from 6 men and 6 women. Find the probabilities that

- (a) there are 2 men and 3 women in the jury, (2 marks)
- (b) there are at least 4 women in the jury, (2 marks)
- (c) there are more men than women in the jury. (2 marks)

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**F.6****Mathematics Paper I (Final Examination 2017-18)**

19. Figure 4(a) shows a piece of square paper  $ABCD$  of length 10 cm.  $E$  and  $F$  are points on  $BC$  and  $DC$  respectively such that  $AF$  bisects  $\angle DAC$  and  $AE$  bisects  $\angle BAC$ .  $B'$  and  $D'$  are points on  $BC$  and  $DC$  respectively such that  $BE = EB' = D'F = FD$ . It is given that  $AC$  intersects  $EF$  and  $B'D'$  at  $I$  and  $J$  respectively.

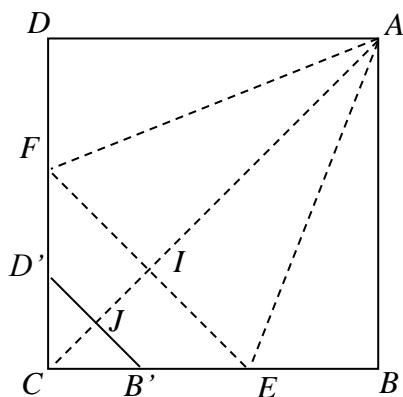


Figure 4(a)

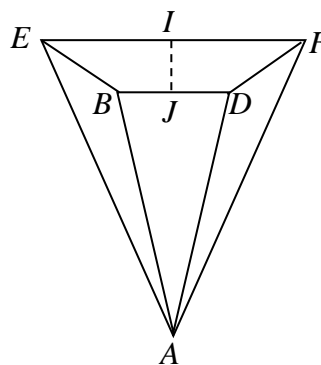


Figure 4(b)

- (a) Find the length of  $DF$ . (2 marks)
- (b) Find the area of  $EB'D'F$  and the length  $IJ$ . (5 marks)
- (c) A piece of pentagonal paper  $ABB'D'D$  is formed by cutting off the triangular part  $B'CD'$  from the square paper  $ABCD$ . The pentagonal paper is folded along  $AE$ ,  $AF$  and  $EF$ , such that  $BE$  and  $DF$  coincide with  $B'E$  and  $D'F$  respectively to form a container as shown in Figure 4(b).
  - (i) Find the angle between the planes  $BDFE$  and  $AFE$ .
  - (ii) Find the capacity of the container. (6 marks)

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