ST. STEPHEN'S GIRLS' COLLEGE Final Examination 2017 - 18

Form 6

126 students

Mathematics Paper I Time allowed : 2¹/₄ hours Question/Answer Paper

Please read the following instructions very carefully.

- 1. Write your class, class number, name and division (if applicable) in the spaces provided on this cover.
- This paper consists of THREE sections, A(1), A(2) and B. Each section carries 35 marks.
- 3. Attempt ALL questions in this paper. Write your answers in the spaces provided in this Question/Answer Paper.
- 4. Graph paper and supplementary answer sheets will be supplied on request. Write your class, class number and name on each sheet, and fasten them with string INSIDE this paper.
- 5. Unless otherwise specified, all working must be clearly shown.
- 6. Unless otherwise specified, numerical answers should either be exact or correct to 3 significant figures.
- 7. The diagrams in this paper are not necessarily drawn to scale.

ClassClass No.NameDivision

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LC, WMC, KAL, SCHL, CYN

	Mathematics Paper I (Final Examination 2017-18)	
	A(1) (35 marks)	
Make	q the subject of the formula $p = \frac{r - 2q}{q + r}$.	(3 marks
	<i>q</i> + <i>i</i>	
<i>.</i>	x ⁻⁸	
Simpli	fy $\frac{x^{-8}}{(x^2y^4)^{-3}}$ and express your answer with positive indices.	(3 marks
Factor		
• •	$a^2-6ab+b^2$,	
(b) 9a	$a^2 - 6ab + b^2 - 66a + 22b$.	(2
		(3 marks)

4. The prices of an apple and an orange are \$3 and \$4.5 respectively. If Susan buys 25 of these fruits for \$90, find the number of oranges bought. (4 marks)

(a) Solve the inequality 2(x-5) < 3x + 8. (b) Write down the least integer satisfying the inequality 2(x-5) < 3x + 8. (3 marks)

5.

6. In Figure 1, the coordinates of point A are (-2, 6). B is the image of A after it has been reflected with respect to the y-axis and then translated 4 units downwards.

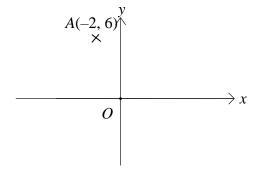


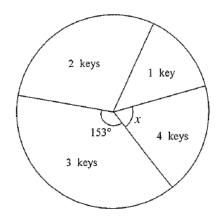
Figure 1

- (a) Write down the coordinates of *B*.
- (b) Is *AB* perpendicular to *OB*? Explain your answer.
- (c) Find the area of $\triangle OAB$.

(5 marks)

7. The pie chart below shows the distribution of the numbers of keys owned by the students in a school. The numbers of students having 2 keys, 3 keys and 4 keys are 60, 85 and k respectively. If a student is randomly selected from the school, then the probability that the

selected student has 4 keys is $\frac{7}{40}$.



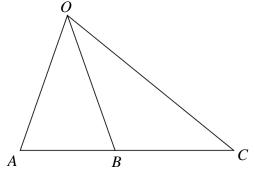
- (a) Find x and k.
- (b) Write down the number of students in the school.

(4 marks)

It is given that y varies inversely as the cube root of <i>x</i> . When <i>x</i> = 125, <i>y</i> = 35. (a) Express <i>y</i> in terms of <i>x</i> . (b) If <i>x</i> is decreased by 27.1%, write down the percentage change of <i>y</i> . (5 mat		Mathematics Paper I (Final Examination 2017-18)	
 (b) If x is decreased by 27.1%, write down the percentage change of y. (5 mather structure) (6 Write down the least possible weight of each paper clip. (7 mather structure) (8 mather structure) (9 mather structure) (10 mather structure) (11 mather structure) (12 mather structure) (13 mather structure) (14 mather struct	It is		
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SECTION A(2) (35 marks)

10. In Figure 2, *B* is a point on *AC* such that OA = OB and $\angle AOB = \angle OCA$.





(a) Prove that $\triangle AOC \sim \triangle BAO$.

(2 marks)

- (b) It is given that OC = 9 cm and AB = 4 cm.
 - (i) Find OA.
 - (ii) If O is the centre of a circle which passes through A and B, is it possible that the area of the sector OAB is less than 11 cm²? Explain your answer. (4 marks)

11. The stem-and-leaf diagram below shows the distribution of a data set *A*. It is known that in the distribution of the data set *A*, the mean, the median and the mode are all equal.

Distribution of data set A								
Stem (ten units)	Le	af (1 uı	nit)				
0	1	4						
1	0	1	Ζ.	6	8			
2	0	0	1	x	х	2	3	9
3	3	7	8					
4	3							

- (a) Find x and z.
- (b) Find the range and the inter-quartile range.
- (c) It is given that the range of another data set *B* is 36 and the inter-quartile range of data set *B* is 16. Determine which data set is more dispersed.

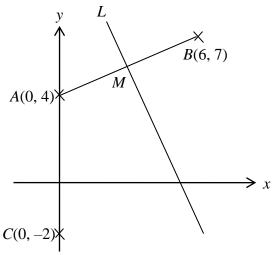
(7 marks)

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- 12. The upper base and the lower base of a right frustum X are squares with sides 12 cm and 18 cm respectively. It is also known that the height of frustum X is 4 cm.
 - (a) Find the volume of frustum *X*. (3 marks)
 - (b) There is another frustum Y which is similar to frustum X. The ratio of the volume of frustum X to the volume of frustum Y is 8 : 27. Find the total surface area of frustum Y. (4 marks)

13. In Figure 3, A(0, 4), B(6, 7) and C(0, -2) are three points on the rectangular coordinate plane. *L* is the perpendicular bisector of *AB* and it intersects *AB* at *M*.





- (a) (i) Find the slope of AB.
 - (ii) Hence, find the equation of *L*.
- (b) P is a point on the rectangular coordinate plane such that PA = PB = PC. Using (a)(ii), find the coordinates of P. (2 marks)
- (c) Let *H* be a moving point on the circle passing through *A*, *B* and *C*. Using (b), find the shortest possible distance between *H* and *M* correct to 2 decimal places. (2 marks)

- 14. Let $f(x) = 1 9x 10x^2 + (ax)^3$. When f(x) is divided by $x + (ax)^2 2$, the quotient and the remainder are 2x 3 and bx + c respectively, where *a*, *b* and *c* are non-zero constants.
 - (a) Find a. (3 marks)
 - (b) Let g(x) be a quadratic polynomial such that when g(x) is divided by $x + (ax)^2 2$, the reminder is -bx-c.
 - (i) Prove that f(x) + g(x) is divisible by $x + (ax)^2 2$.
 - (ii) Someone claims that all the roots of the equation f(x) + g(x) = 0 are rational numbers. Do you agree? Explain your answer. (5 marks)

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SECTION B (35 marks)

15. Let *a* and *b* be constants. Denote the graph of $y = \log_a x + b$ by *G*. The *x*-intercept of *G* is 16 and *G* passes through the point (64, 2). Express *x* in terms of *y*. (4 marks)

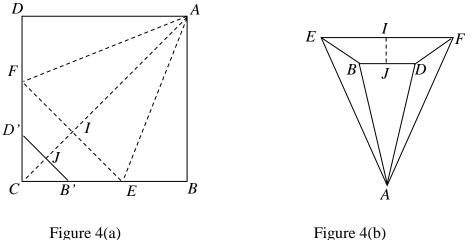
- 16. A country adopts a plan to import crude oil from another country. It is given that the volume of crude oil imported in the 1st year since the start of the plan is 8×10^7 m³ and in subsequent years, the volume of crude oil imported each year is 10% less than the volume of crude oil imported in the previous year.
 - (a) Find the total volume of crude oil imported in the first 10 years since the start of the plan. (2 marks)
 - (b) Find the least value of *n* such that the total volume of crude oil imported in the first *n* years since the start of the plan exceeds 7×10^8 m³. (2 marks)

- 17. A jury of 5 is chosen at random from 6 men and 6 women. Find the probabilities that
 - (a) there are 2 men and 3 women in the jury,
 (b) there are at least 4 women in the jury,
 (c) there are more men than women in the jury.
 (2 marks)
 (2 marks)

- 18. The equation of the parabola Γ is $y = -x^2 + mx$, where *m* is a real constant. Denote the straight line y = x + 9 by *L*.
 - (a) If the points of intersection of L and Γ are A(a, p) and B(b, q), express $(a b)^2$ in terms of m. (3 marks)
 - (b) If L touches Γ at the point Q,
 - (i) find the value(s) of *m* by using the result in (a),
 - (ii) find the coordinates of Q.

(5 marks)

19. Figure 4(a) shows a piece of square paper ABCD of length 10 cm. E and F are points on BC and DC respectively such that AF bisects $\angle DAC$ and AE bisects $\angle BAC$. B' and D' are points on BC and DC respectively such that BE = EB' = D'F = FD. It is given that AC intersects EF and B'D' at I and J respectively.





(2 marks)

(5 marks)

(6 marks)

- (a) Find the length of *DF*.
- (b) Find the area of *EB* '*D* '*F* and the length *IJ*.
- A piece of pentagonal paper ABB'D'D is formed by cutting off the triangular part (c) B'CD' from the square paper ABCD. The pentagonal paper is folded along AE, AF and EF, such that BE and DF coincide with B'E and D'F respectively to form a container as shown in Figure 4(b).
 - (i) Find the angle between the planes *BDFE* and *AFE*.
 - (ii) Find the capacity of the container.

End of Paper